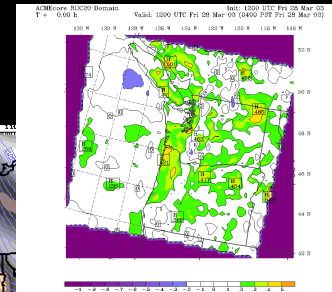
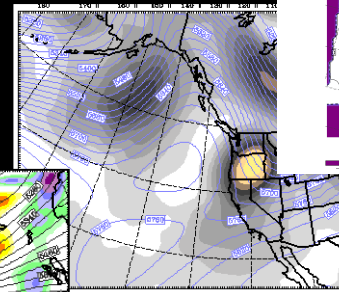
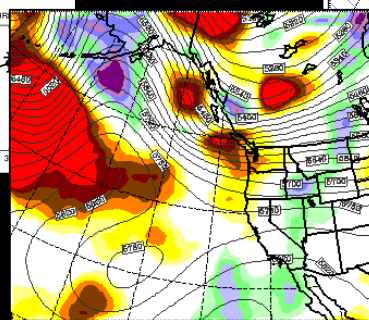
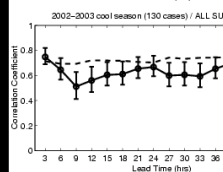
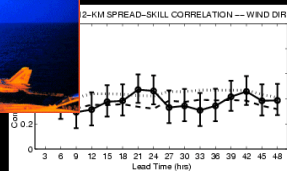


# Toward Short-Range Ensemble Prediction of Mesoscale Forecast Error

Eric P. Grit and Clifford F. Mass  
University of Washington

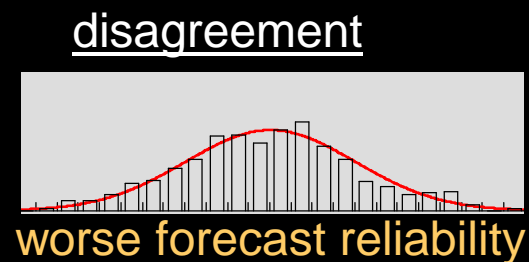
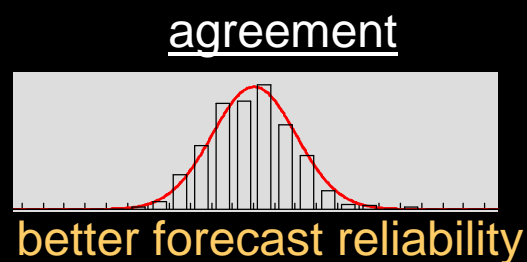


Supported by:  
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A Consortium of Federal and Local Agencies



## Traditional Approach – Spread-Error Correlation

- Ensemble spread should provide an approximation to the true forecast uncertainty

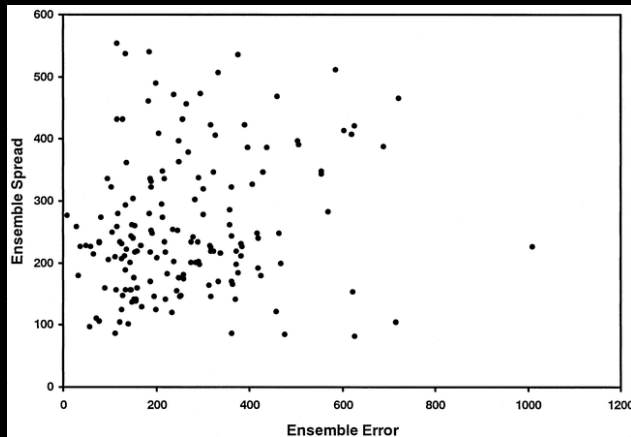


- To quantify this “spread-skill relationship”:
  - Find the linear correlation between ensemble spread ( $\sigma$ ) and the ensemble mean forecast error ( $|e_{EM}|$ ) over a large sample
  - Strength of the correlation is limited by the case-to-case spread variability ( $\beta$ ) (Houtekamer, 1993; Whitaker and Lough, 1998)

$$\rho^2(\sigma, |e_{EM}|) = \frac{2}{\pi} \frac{1 - \exp(-\beta^2)}{1 - \frac{2}{\pi} \exp(-\beta^2)}; \beta = \text{std}(\ln \sigma)$$

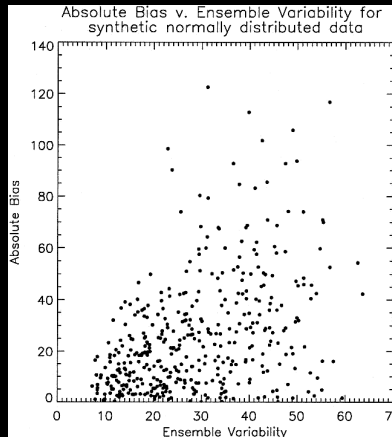
# Observed Forecast Error Predictability: A Disappointment

Tropical Cyclone Tracks



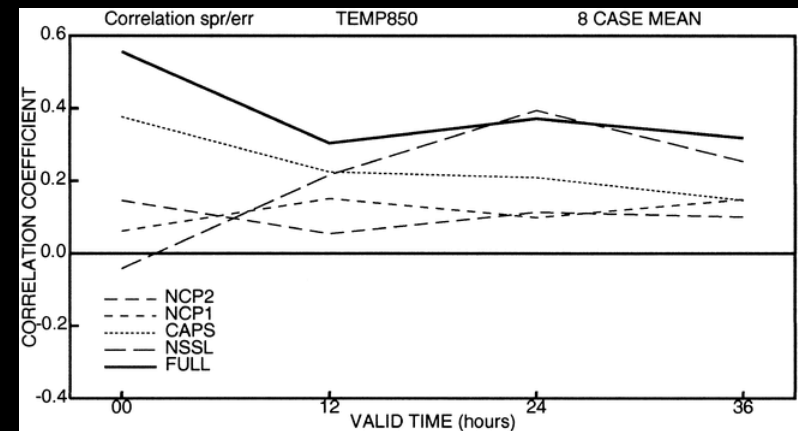
[c.f. Goerss 2000]

NCEP SREF Precipitation



[c.f. Hamill and Colucci 1998]

SAMEX '98 SREFs



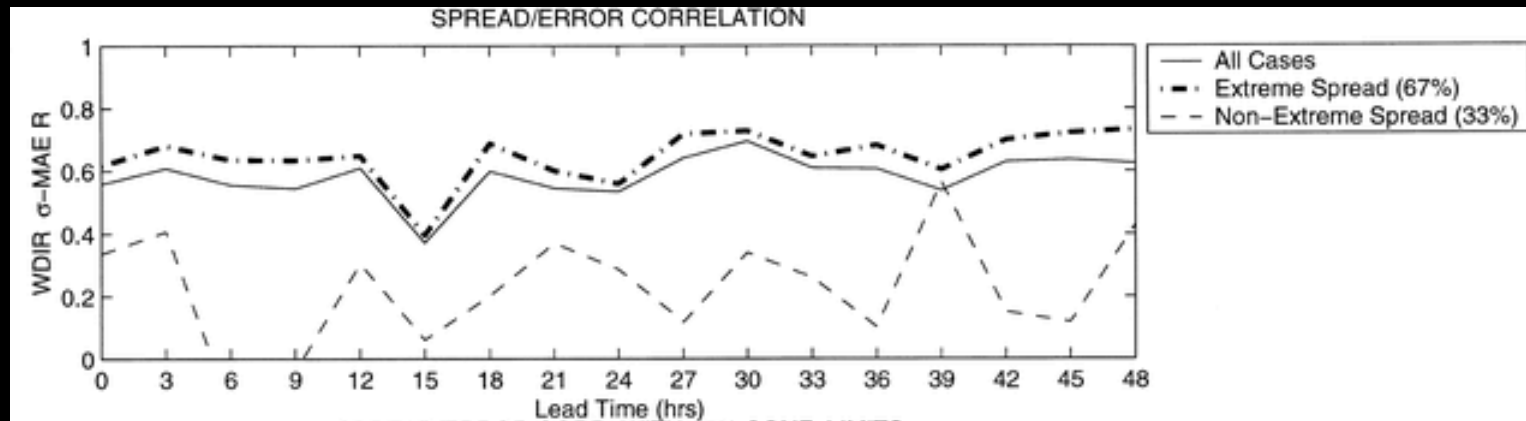
[c.f. Hou et al. 2001]

- Highly scattered relationships, thus low correlations
- No indication of spread-error correlation potential
- No assessment of dependency on the metrics used

## Observed Forecast Error Predictability: A Disappointment

Not all hope is lost...

UW MM5 SREF 10-m Wind Direction



[c.f. Grit and Mass 2002]

- **More recent studies show that domain-averaged spread-error correlations can be as high as 0.6-0.7**  
(Grit and Mass 2002, Stensrud and Yussouf 2003)
- **Potentially higher correlations can be achieved by considering only cases with extreme spread**

# A Simple Stochastic Model of Spread-Skill

## PURPOSES:

- 1) To establish practical limits of forecast error predictability, that could be expected given perfect ensemble forecasts of finite size.
- 2) To address the user-dependent nature of forecast error estimation by employing a variety of predictors and error metrics.

## A Simple Stochastic Model of Spread-Skill

1. Draw today's "forecast uncertainty" from a log-normal distribution (Houtekamer 1993 model).

$$\ln(\sigma) \sim N(\ln(\sigma_f), \beta^2)$$

2. Create synthetic ensemble forecasts by drawing  $M$  values from the "true" distribution.

$$F_i \sim N(Z, \sigma^2) ; i = 1, 2, \dots, M$$

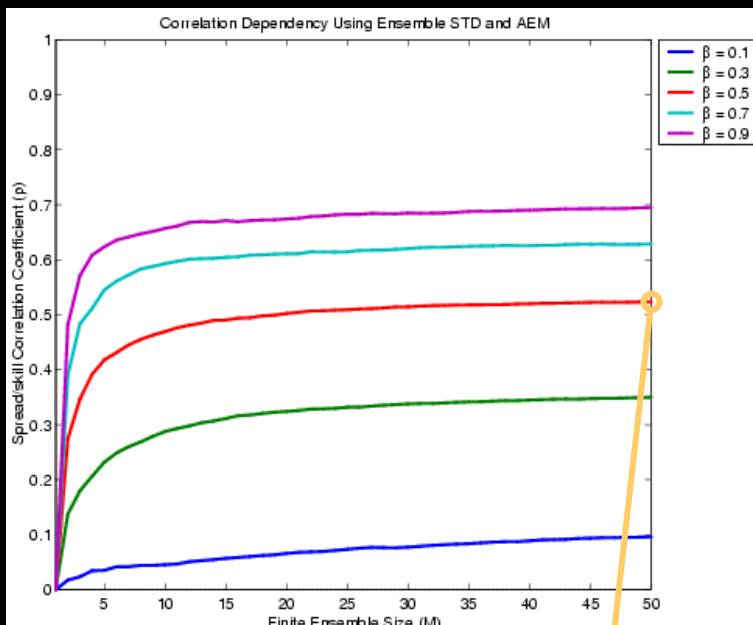
3. Draw the verifying observation from the same "true" distribution (statistical consistency).

$$V \sim N(Z, \sigma^2)$$

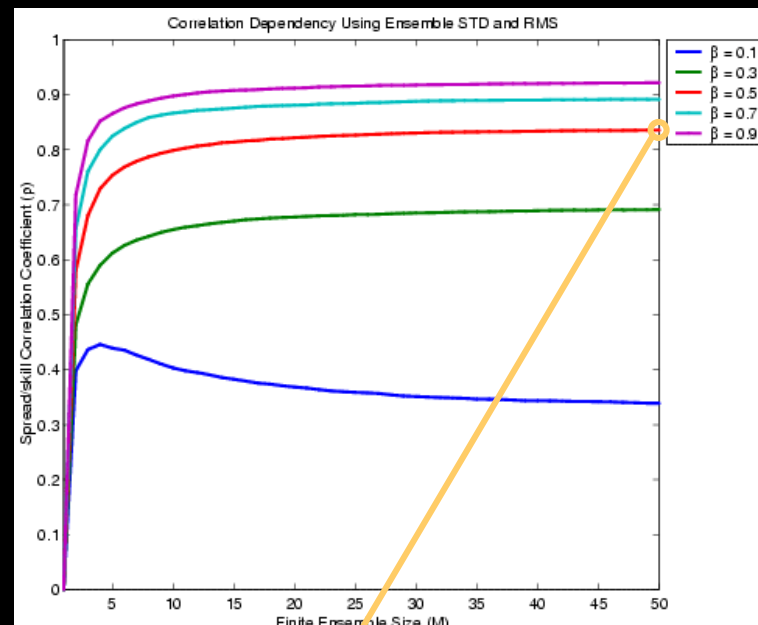
- Stochastically simulated ensemble forecasts at a single, arbitrary observing location or model-grid box with 50,000 realizations (cases)
- Assumed:
  - Gaussian statistics
  - statistically consistent (perfectly reliable) ensemble forecasts
- Varied:
  - temporal spread variability ( $\beta$ )
  - finite ensemble size ( $M$ )
  - spread and skill metrics (continuous and categorical)

# Simple Model Spread-Error Correlations

STD-AEM correlation

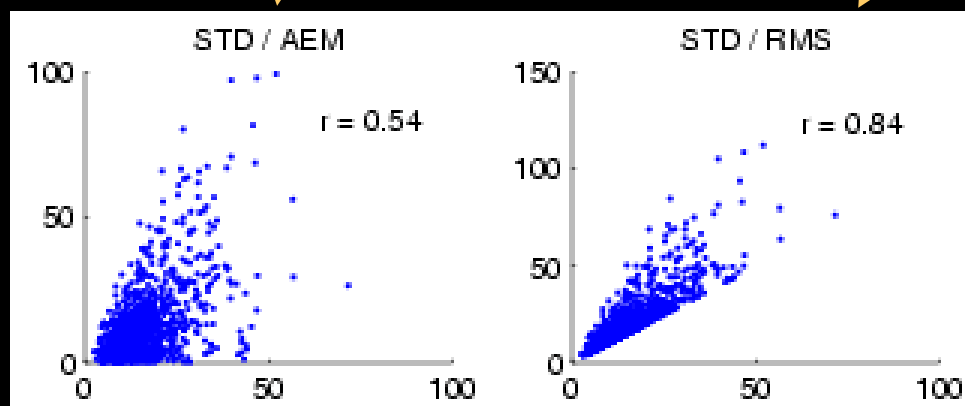


STD-RMS correlation



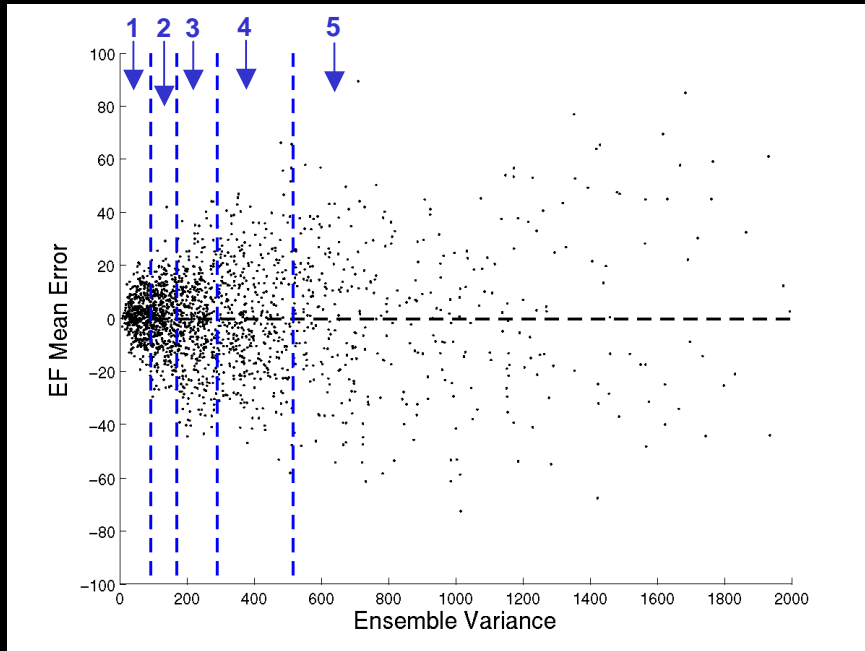
spread  
STD = Standard  
Deviation

error  
RMS= Root-Mean  
Square error  
AEM= Absolute Error  
of the ensemble  
Mean



$\beta = 0.5$ ;  
 $M = 50$

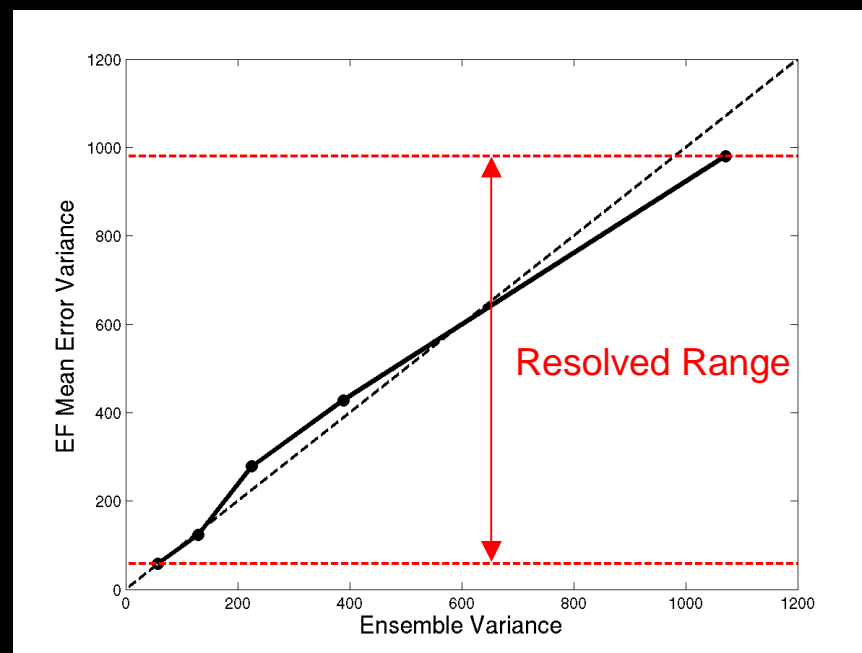
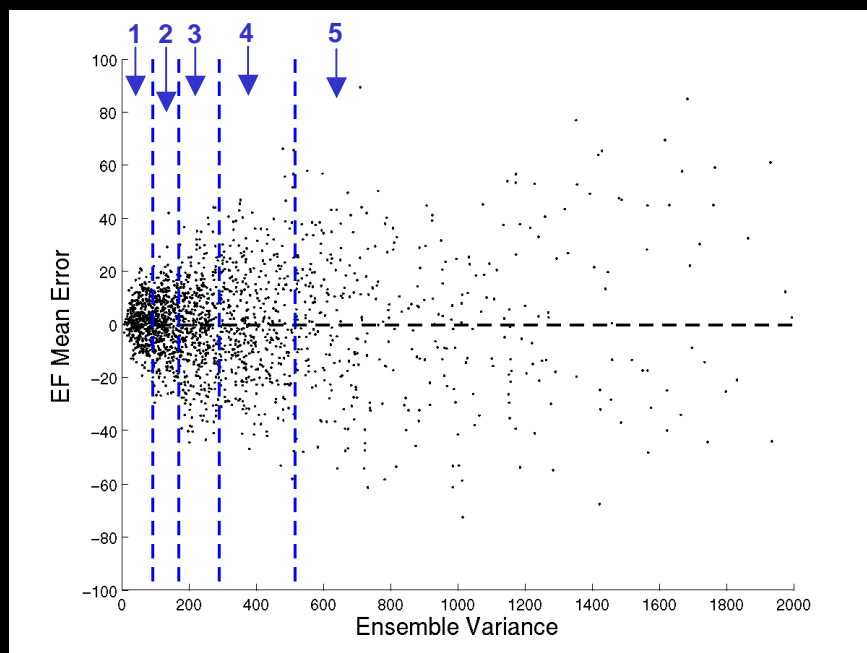
## Alternative Approaches



**Given statistical consistency, ensemble variance should equal the EF mean forecast error variance.**



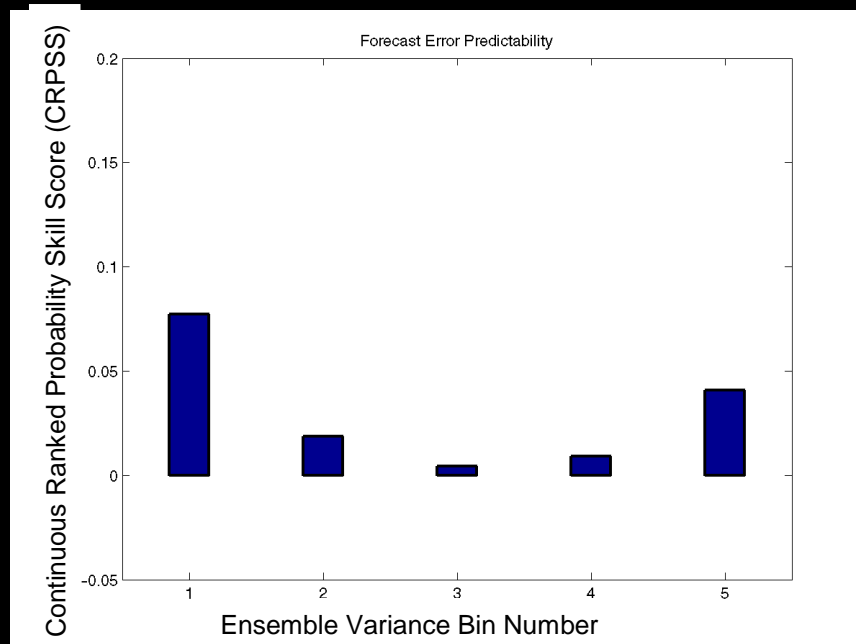
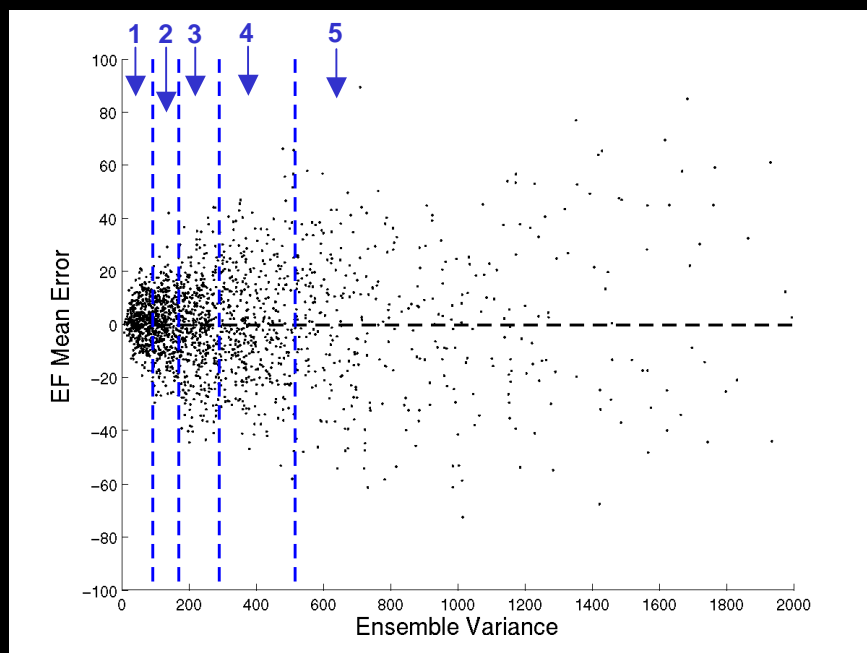
## Alternative Approaches



### ■ Resolved range of error variance (Wang and Bishop 2003)

- Choose  $N_{bin}$  equally populated bins of ensemble variance
- Find the mean ensemble variance and the error variance within each bin
- The range of resolved error variances indicates closeness to statistical consistency
- Could also be applied to other error metrics (e.g. AEM, RPS)

## Alternative Approaches



### ■ Probabilistic skill of forecast error predictions

- Use errors conditioned by spread category as probabilistic predictions of forecast error.
  - Evaluate using CRPS and its associated skill score with a cross-validation procedure.
  - CRPSS measures the continuous forecast error predictability.
- For categorical error forecasts, use BS or RPS and the associated skill score.
- Tradeoff between bin widths and number of samples in each bin.

## UW SREF System Summary

Imported Homegrown	Name	# of Members	EF Type	Initial Conditions	Forecast Model(s)	Forecast Cycle	Domain
	ACME	17	SMMA	8 Ind. Analyses, 1 Centroid, 8 Mirrors	“Standard” MM5	00Z	36km, 12km
	ACME <sup>core</sup>	8	SMMA	Independent Analyses	“Standard” MM5	00Z	36km, 12km
	ACME <sup>core+</sup>	8	PMMA	“ “	8 MM5 variations	00Z	36km, 12km
	PME	8	MMMA	“ “	8 “native” large-scale	00Z, 12Z	36km

ACME: Analysis-Centroid Mirroring Ensemble

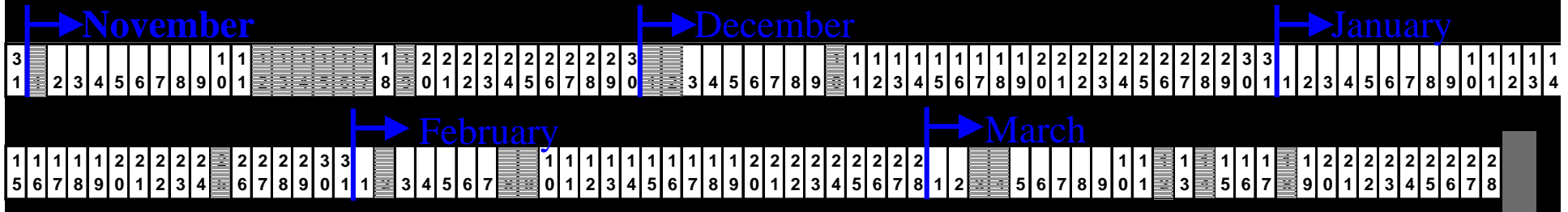
PME: Poor-Man’s Ensemble

SMMA: Single-Model Multi-Analysis

PMMA: Perturbed-Model Multi-Analysis

MMMA: Multi-model Multi-Analysis

# Mesoscale SREF and Verification Data



## ■ Mesoscale SREF Data:

- Total of 129, 48-h forecasts (31 OCT 2002 – 28 MAR 2003) all initialized at 0000 UTC
- Missing forecast case days are shaded
- Parameters of Focus:
  - 12 km Domain: Wind @ 10m ( $WDIR_{10}$ ,  $WSPD_{10}$ ), Temperature at 2m ( $T_2$ )
- Short-term mean bias correction
  - Applied at every location and forecast lead time separately
  - Varied training window from 2-30 days

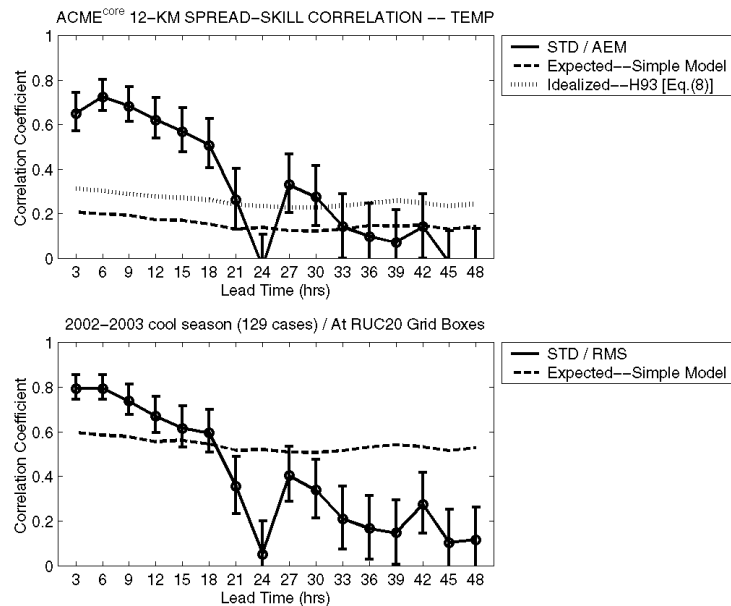
## ■ Verification Data:

- 12 km Domain: RUC20 analysis  
(NCEP 20 km mesoscale analysis)  
observations

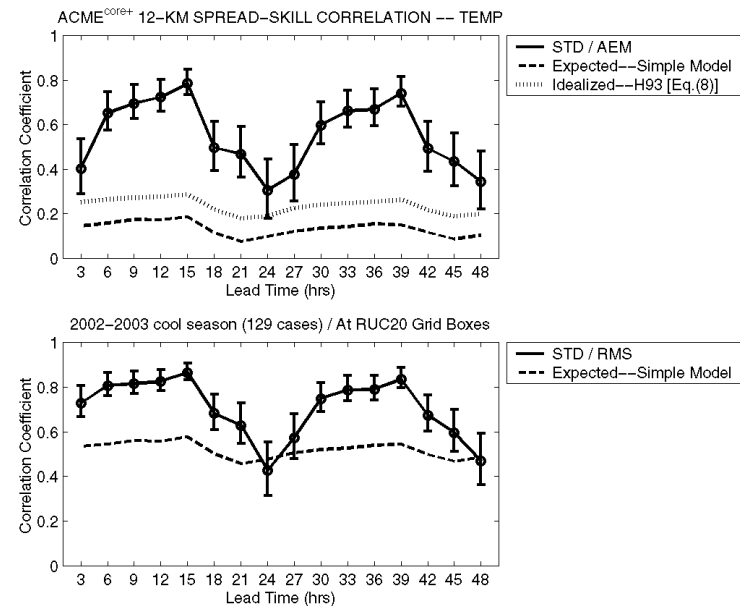
# Domain-Averaged Spread-Error Correlation

(no bias correction)

ACME<sub>core</sub>



ACME<sub>core+</sub>



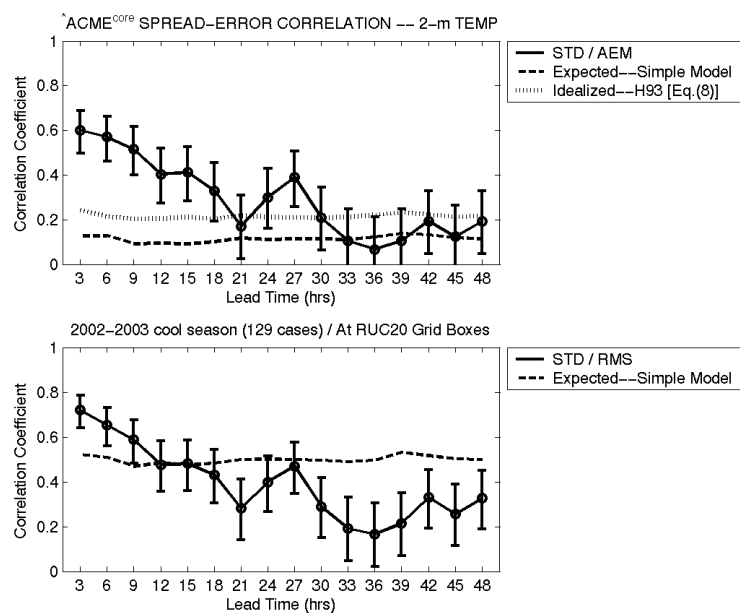
- The benefit of including model physics variability is apparent.
- Domain-averaging produces correlations much higher than expected. Correlations of averages are referred to as *ecological correlations* in statistics.



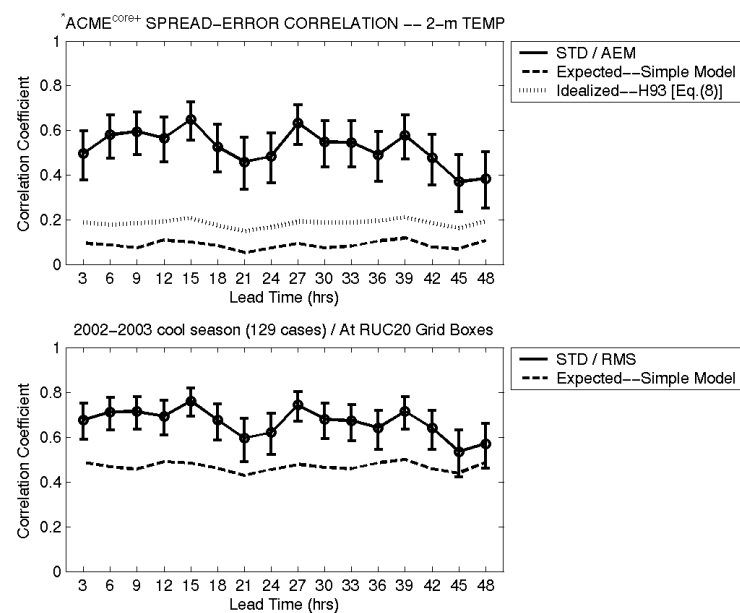
# Domain-Averaged Spread-Error Correlation

(14-day bias correction)

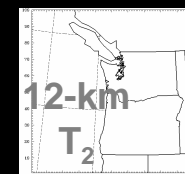
\*ACME<sub>core</sub>



\*ACME<sub>core+</sub>

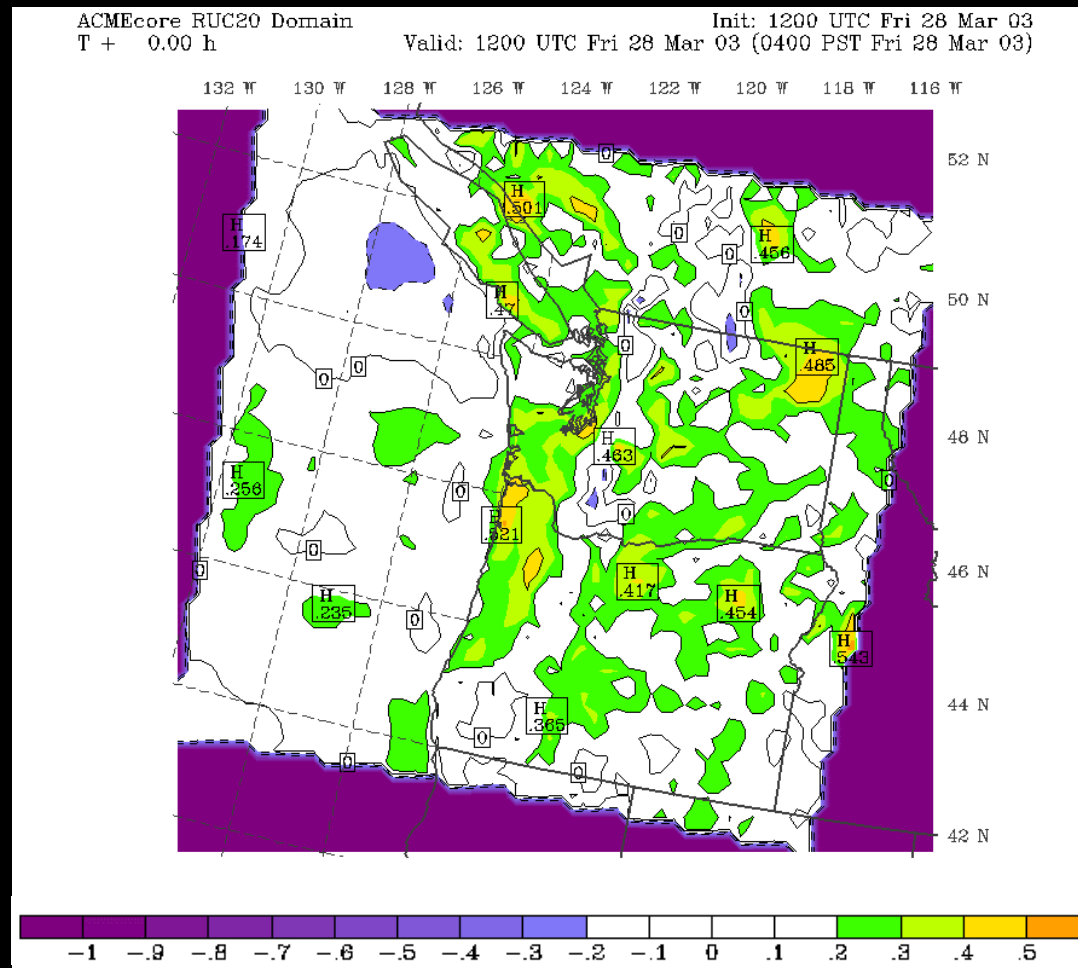


- Bias correction reduces case-to-case spread variability, resulting in poorer spread-error correlations overall.



# Spatial Distribution of Local Spread-Error Correlation

Domain-Averaged  
STD-AEM correlation  
~ 0.62

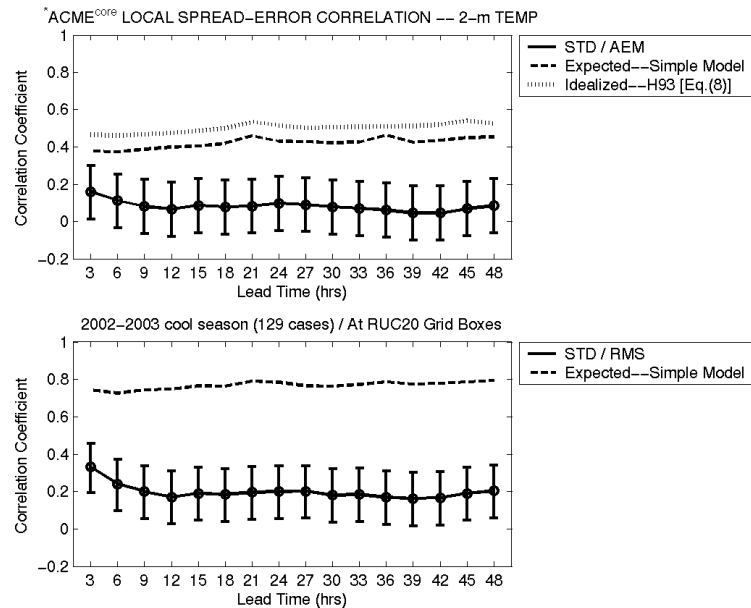


Maximum Local  
STD-AEM correlation  
~ 0.54

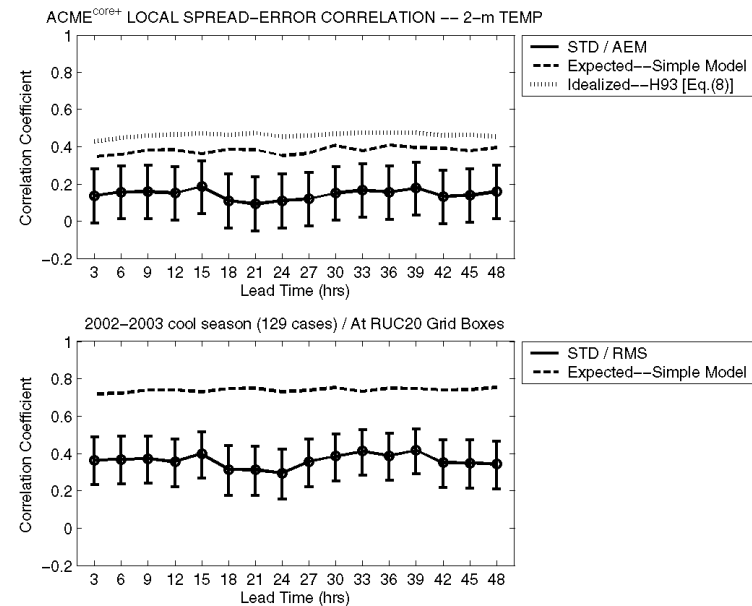
# Average Local Spread-Error Correlation

(no bias correction)

ACME<sup>core</sup>



ACME<sup>core+</sup>



- The average local spread-error correlations are small.
- Estimates from the simple stochastic model are more applicable here, giving an indication of the departure from local statistical consistency.





## Preliminary Conclusions

- Accounting for model and surface boundary parameter uncertainty in a mesoscale SREF system is crucial.
  - ACME<sup>core+</sup> forecasts possess valuable information about the flow-dependent mesoscale uncertainty that ACME<sup>core</sup> forecasts do not.
- Eckel and Mass (2003) found that a simple bias correction improves ensemble forecast skill, but these results suggest that degradations are also possible.
  - Traditional spread-error correlations are reduced in many cases
  - A shorter range of error variances are resolved (F00-F15)
- Continuous (categorical) predictors of forecast error are most appropriate for end users with a continuous (categorical) utility function.

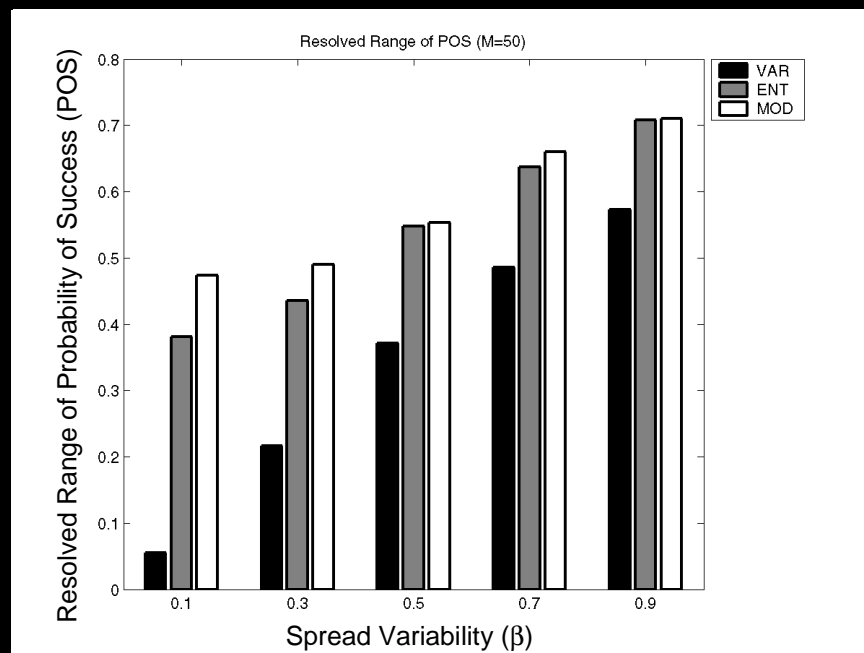
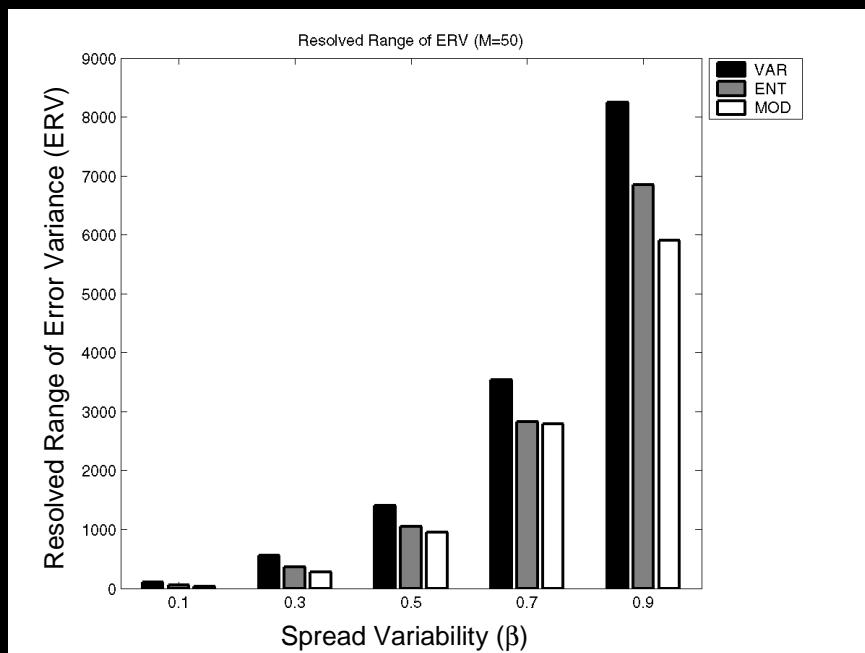
## Outstanding Questions

- How can an ensemble-based prediction system for local forecast errors be developed?
  - Ecological (domain-averaged) spread-error correlations can be quite large, while local spread-error correlations are near zero.
  - Can we ever expect local statistical consistency?
- Will more sophisticated post-processing methods (e.g. – ensemble MOS, best-member dressing, Bayesian model averaging) also degrade the forecast error predictability?
  - Or is the decrease in forecast error predictability in this study an aberration?
  - Maintaining case-to-case spread variability must be a constraint of paramount importance for ensemble post-processing methods.

## FURTHER QUESTIONS???

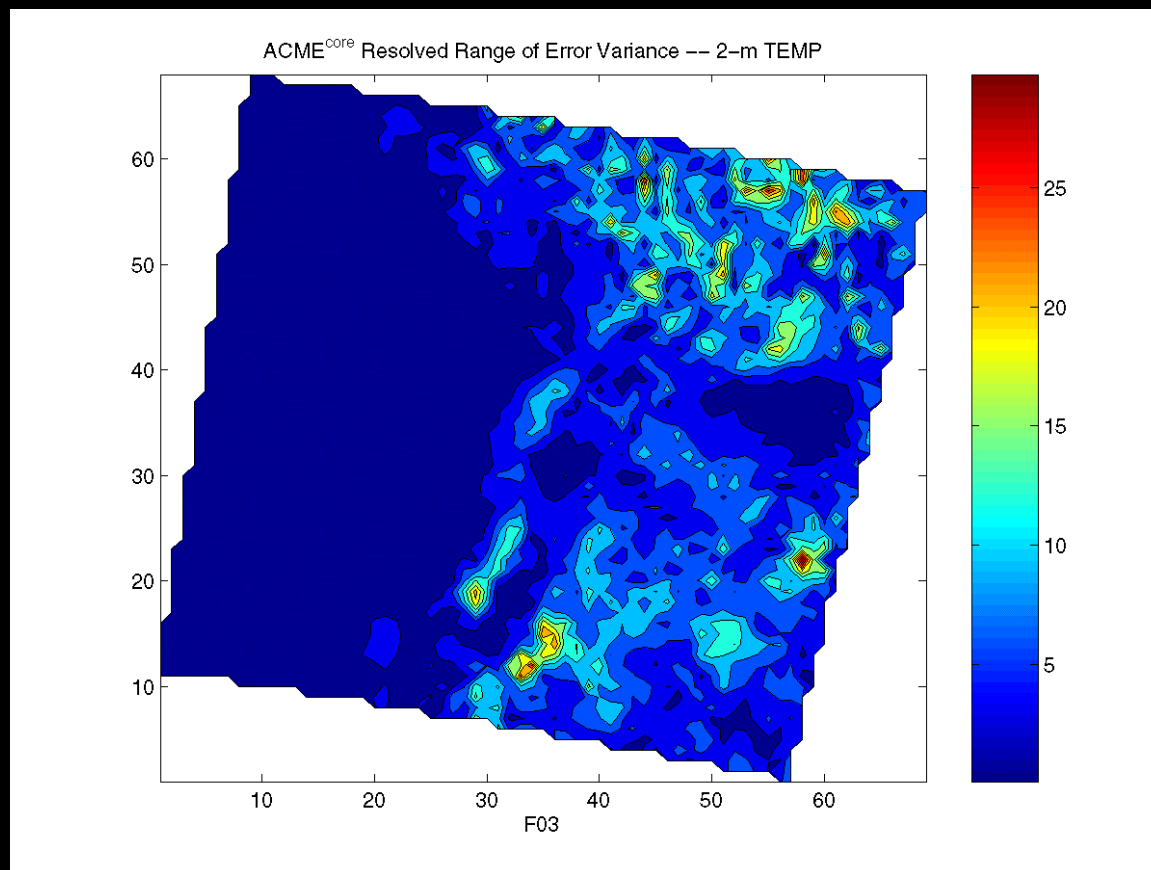
## EXTRA SLIDES

## Continuous or Categorical Predictors?



- Continuous (categorical) predictors of forecast error are most skillful for end users with a continuous (categorical) utility function.

## Spatial Distribution of Resolved Range of ERV

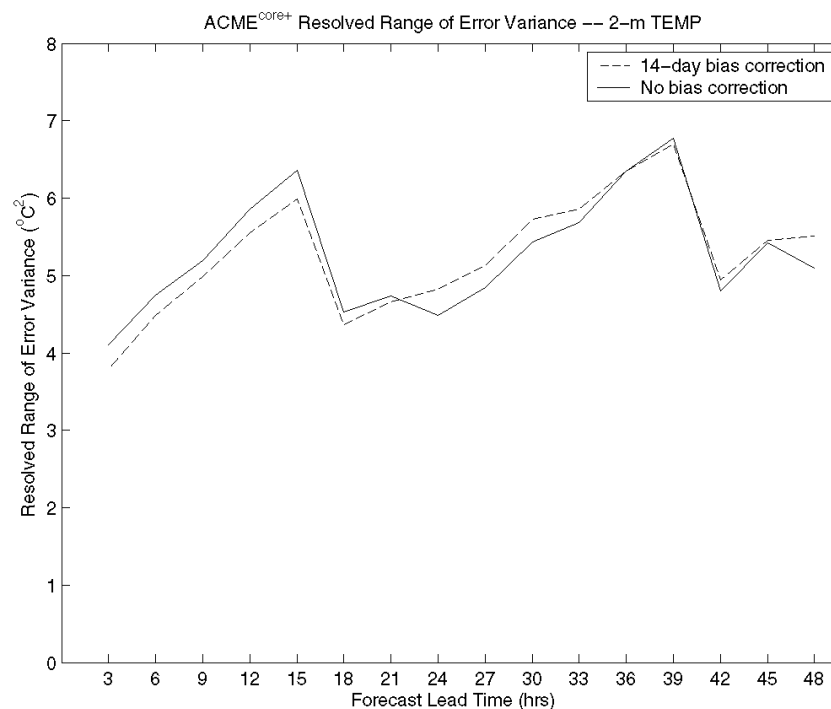
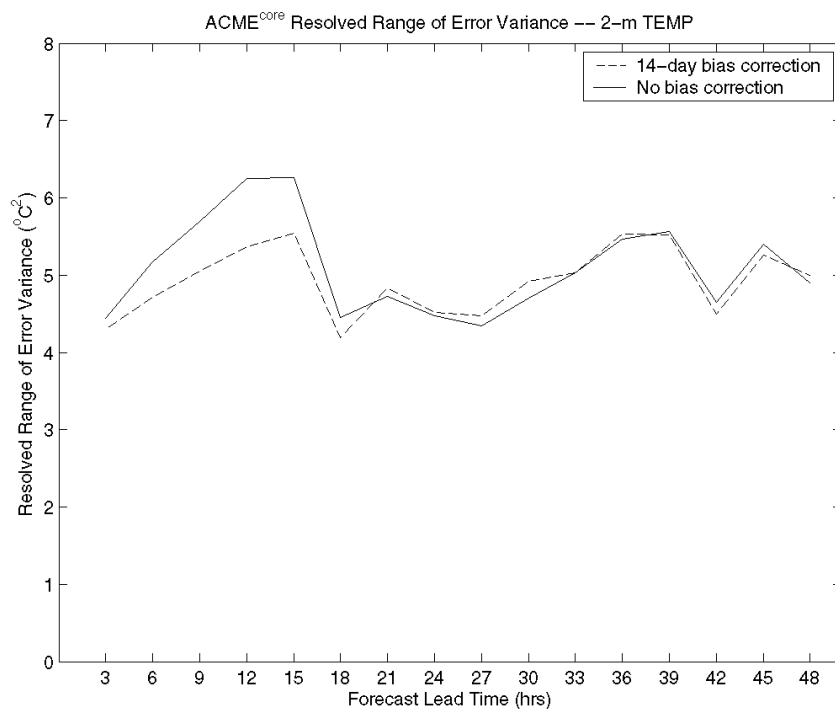


# Resolved Range of Local Error Variance

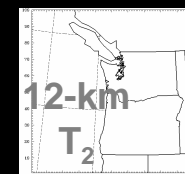
(Domain-averaged)

ACME<sup>core</sup>

ACME<sup>core+</sup>



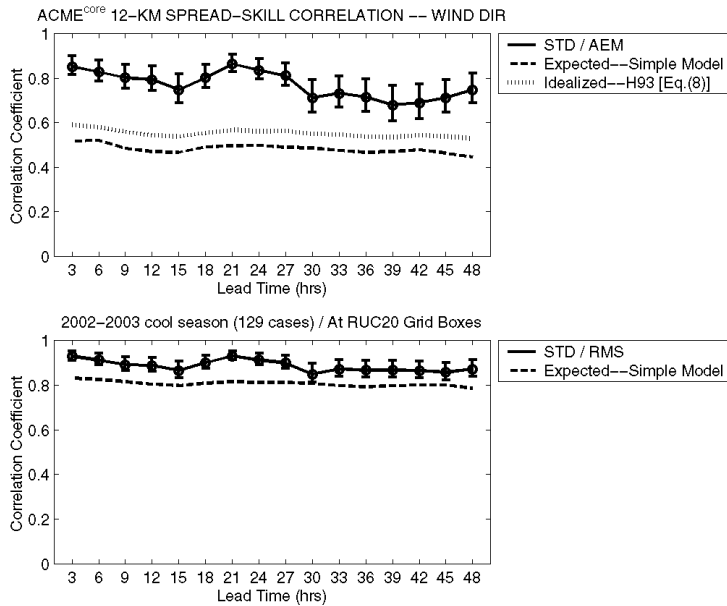
- Bias correction reduces the resolved range of local error variances during the first 15h. At longer lead times, no difference is apparent.



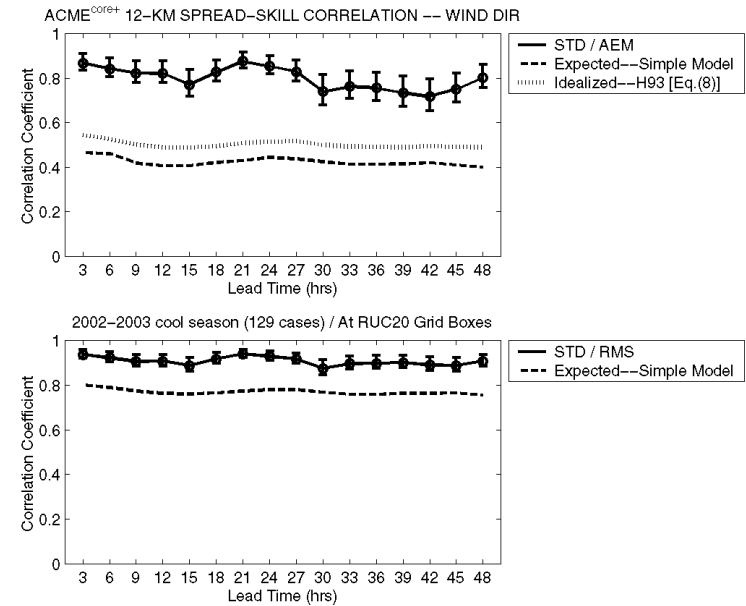
# Spread-Error Correlations

(no bias correction)

ACME<sup>core</sup>



ACME<sup>core+</sup>



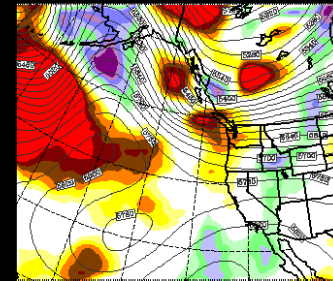
## Forecast Error Prediction

- Like any other scientific prediction or measurement, weather forecasts should be accompanied by error bounds, or a statement of uncertainty.

$$T_{2m} = 3\text{ }^{\circ}\text{C} \pm 2\text{ }^{\circ}\text{C} \quad P(T_{2m} < 0\text{ }^{\circ}\text{C}) = 6.7\%$$

- Forecast uncertainty changes spatially and temporally, and is dependent on:

- Atmospheric predictability – a function of the sensitivity of the flow to:
  - Magnitude/orientation of initial state errors
  - Numerical model errors / deficiencies



- Ensemble weather forecasts appear well-suited for quantifying fluctuations in atmospheric predictability



## Value of Forecast Error Prediction

- Operational forecasters require explicit prediction of this flow-dependent forecast uncertainty
  - Helps to decide how much to trust model forecast guidance
  - Current uncertainty knowledge is partial, and largely subjective
- End users could greatly benefit from knowing the expected forecast error
  - Allows sophisticated users to make optimal decisions in the face of uncertainty (economic cost-loss or utility)

Take protective action if:  $P(|E_{T_{2m}}| > 2\text{ }^{\circ}\text{C}) > \text{cost/loss}$

- Common users of weather forecasts – confidence index

